

Quantum Alchemy and PECD

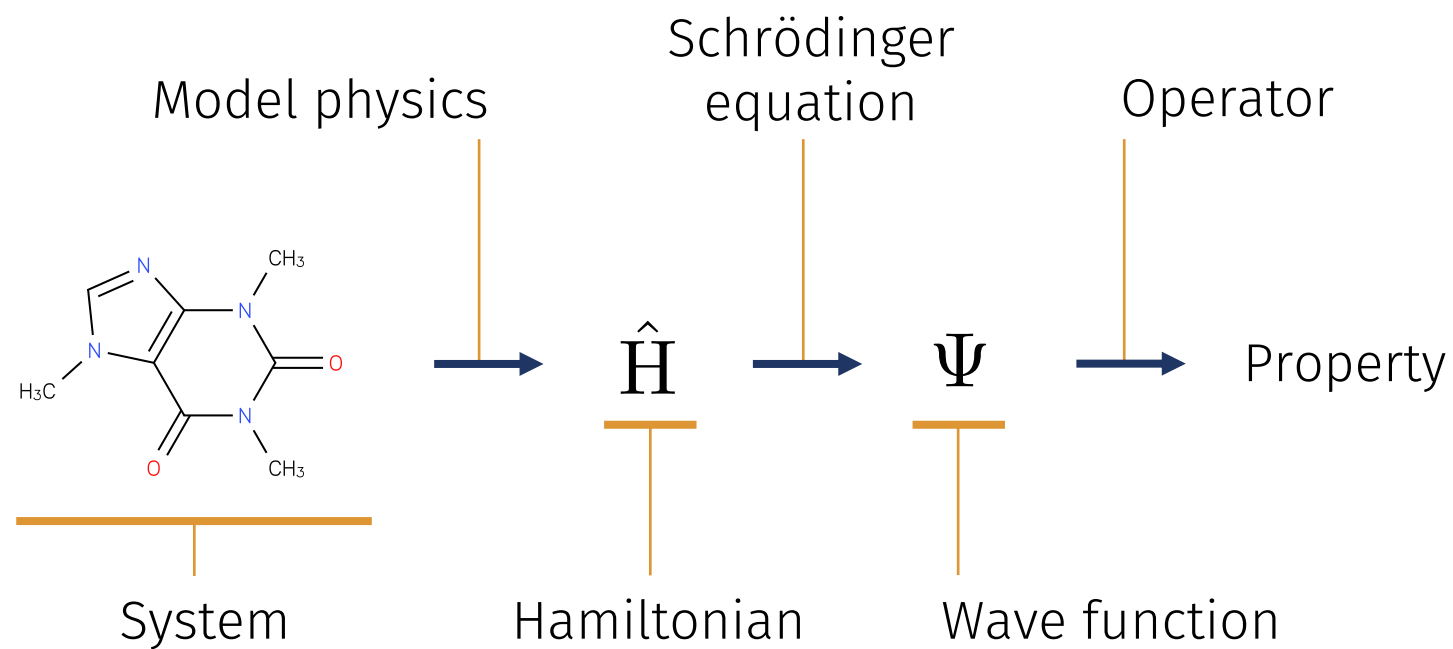
Guido Falk von Rudorff, University of Kassel

 vonrudorff@uni-kassel.de

 nablachem.org/talks

 [ferchault](https://github.com/ferchault)

 [@ferchault](https://twitter.com/ferchault)



Idea

Treat system changes perturbatively^[1,2]
Build a Taylor/Padé approximant^[3]: often 100.000 times faster

Steps

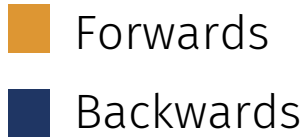
Choose system



Alter system, calculate property response functions

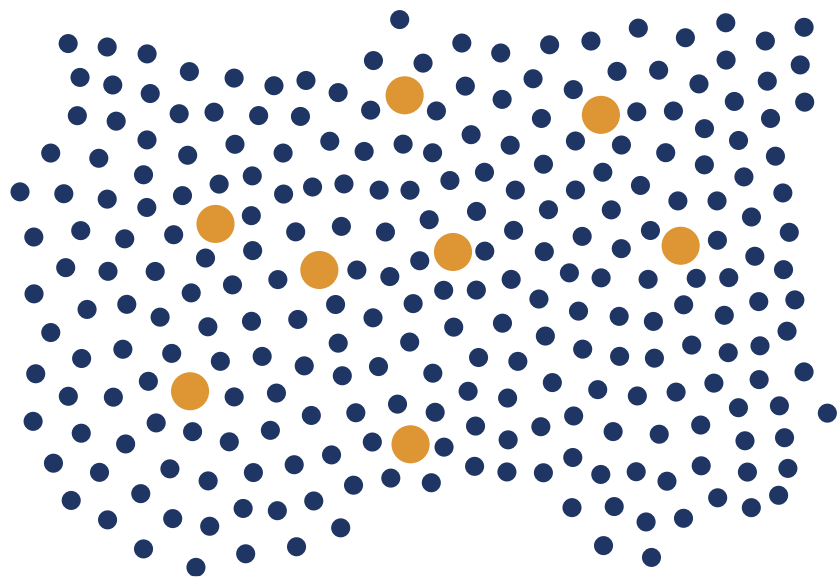


Predict many modified systems

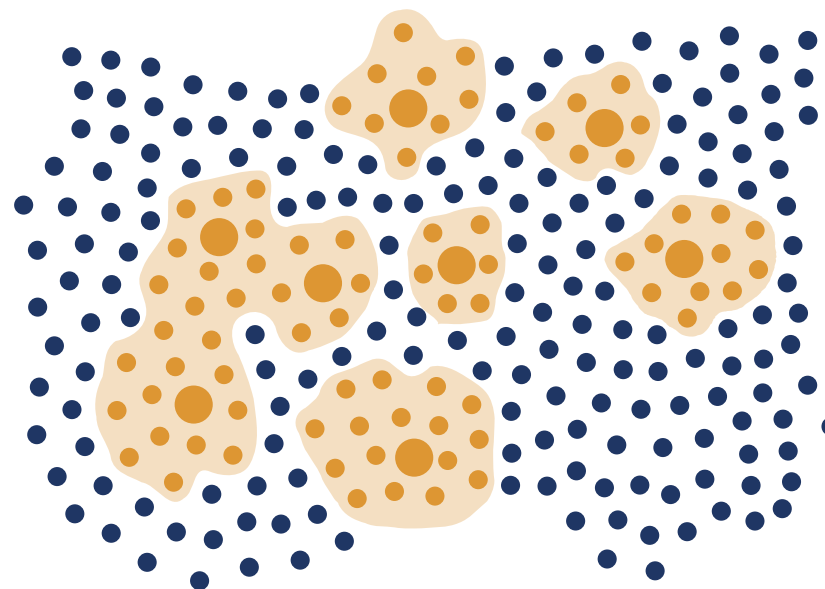


1 | E. B. Wilson, *J. Chem. Phys.* 1962. 2 | GFvR, O. A. von Lilienfeld, *Phys. Rev. Res.*, 2020. 3 | GFvR, *J. Chem. Phys.*, 2021.

Without Perturbation



With Perturbation



- Systems
- Any
 - Known
 - Approximated

Perspective shift

Few highly accurate calculations
instead of many intermediate ones

$$\hat{H} = \hat{H}(\underbrace{Z_i}_{4N}, \underbrace{\mathbf{R}_i}_{1D, \text{ close to } \sum_i Z_i}, \underbrace{N_e}_{1D}, \sigma)$$

Differentiable / Analytic

- ✓ Total Energy ^[1,2]
- ✓ Dipole moments ^[2]
- ✓ Deprotonation energies ^[3]
- ✓ Electron density ^[1,2]
- ✓ Non-covalent interactions ^[1]
- ✓ Ionisation Energy ^[4]
- ✓ Orbital eigenvalues ^[2]
- ✓ Binding energies ^[1,2]
- ✓ Electron Affinity ^[4]

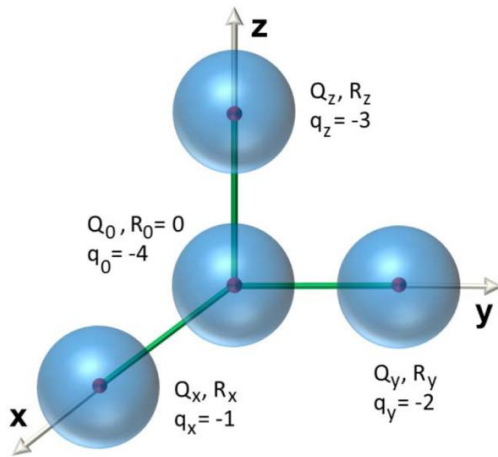
Converge quickly

Angular emission in photoelectron circular dichroism?

1 | GFvR, O. A. von Lilienfeld, *Phys. Rev. Res.*, 2020. 2 | GFvR, *J. Chem. Phys.*, 2021. 3 | GFvR, O. A. von Lilienfeld, *Phys. Chem. Chem. Phys.*, 2020. 4 | E Eikey, A Maldonado, C Griego, GFvR, J Keith, *J. Chem. Phys.*, 2022.

Angular emission

- Expensive to calculate
- Highly coupled degrees of freedom: multidimensional expansion



$$\frac{d\sigma^\pm}{d\Omega} = \frac{\sigma}{4\pi} \left[1 \pm \underbrace{\beta_1 P_1(\cos \theta)}_{\text{dichroic parameter}} - \frac{1}{2} \underbrace{\beta_2 P_2(\cos \theta)}_{\text{anisotropy parameter}} \right]$$

Data

- 85 pairs of β_i
- Center: $Q_{xyz}=2.5$, $R_{xyz} = 3$, photoelectron = 6 eV

$$\beta_i(\mathbf{x}) \simeq \sum_{|\alpha| \leq k} \frac{\partial^{|\alpha|} \beta_i(\mathbf{a})}{\partial x_1^{\alpha_1} \dots \partial x_n^{\alpha_n}} \frac{(\mathbf{x} - \mathbf{a})^\alpha}{\alpha!}$$

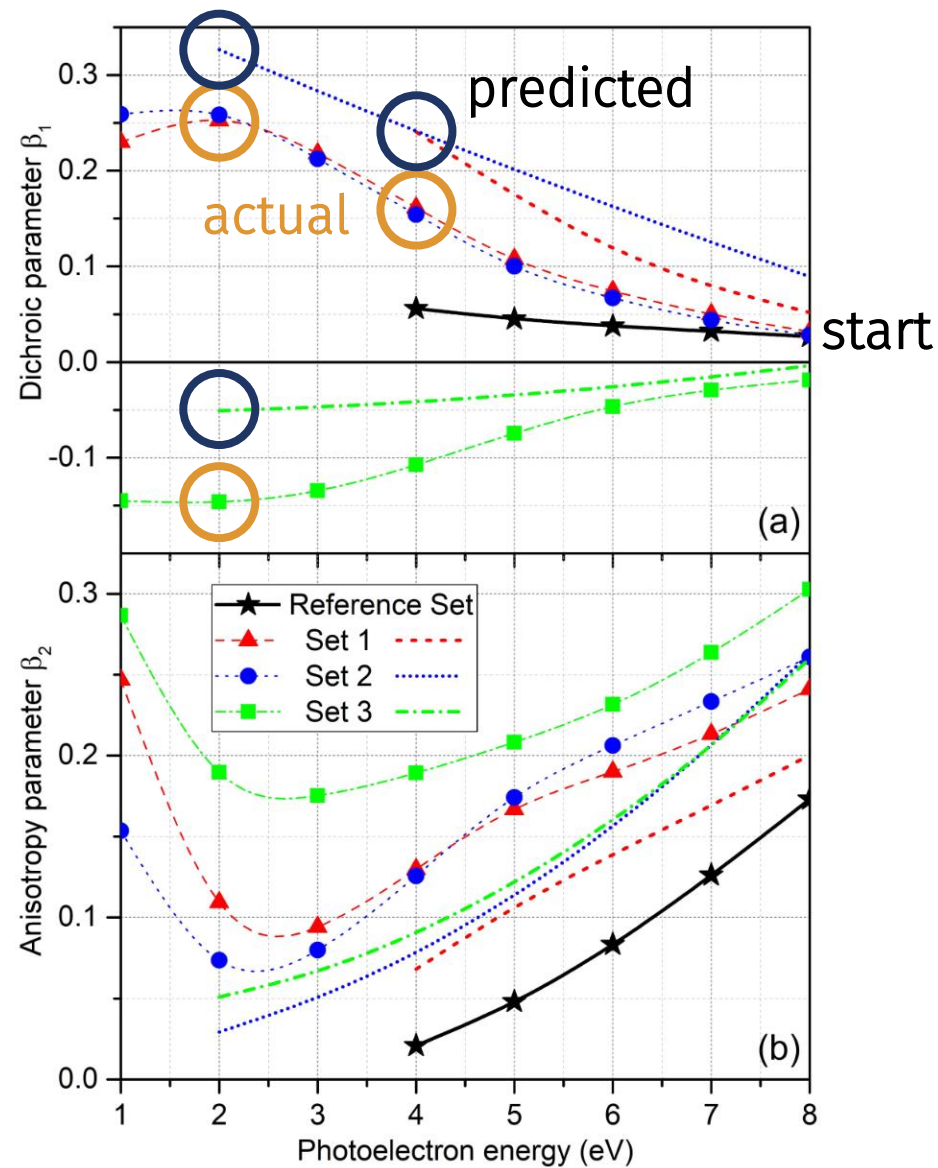
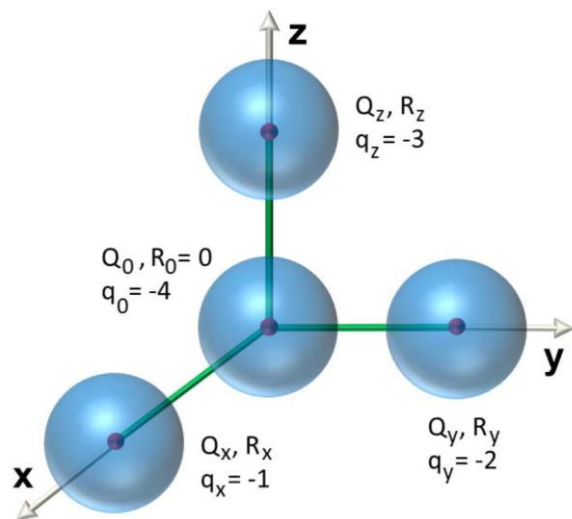
Optimization

Objective

- Modify **all** Q_i, R_i , photoelectron energy
- Find extremal β_1 , predict matching β_2

Results

- max β_1 : 5.6% \rightarrow 25.8%
- Min β_1 : 5.6% \rightarrow -14.7%



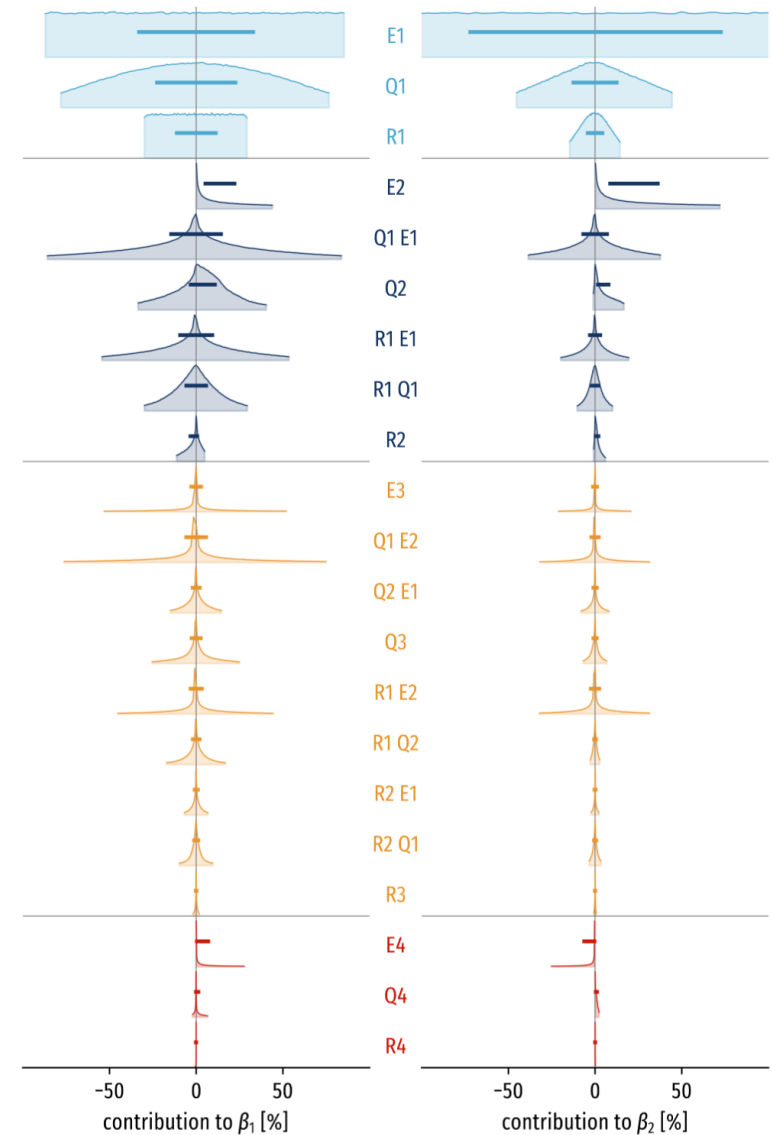
Group terms

- Q_j : Q
- R_j : R
- photoelectron energy: E
- Mixed: count groups

$\frac{\partial \beta_i}{\partial R_x}$	$\frac{\partial^2 \beta_i}{\partial Q_y^2}$	$\frac{\partial^2 \beta_i}{\partial R_x Q_y}$
$\in R1$	$\in Q2$	$\in R1 Q1$

Results

- Converges quickly
- Few third order terms contribute
- Almost no spatial-spatial coupling



Relate to cost

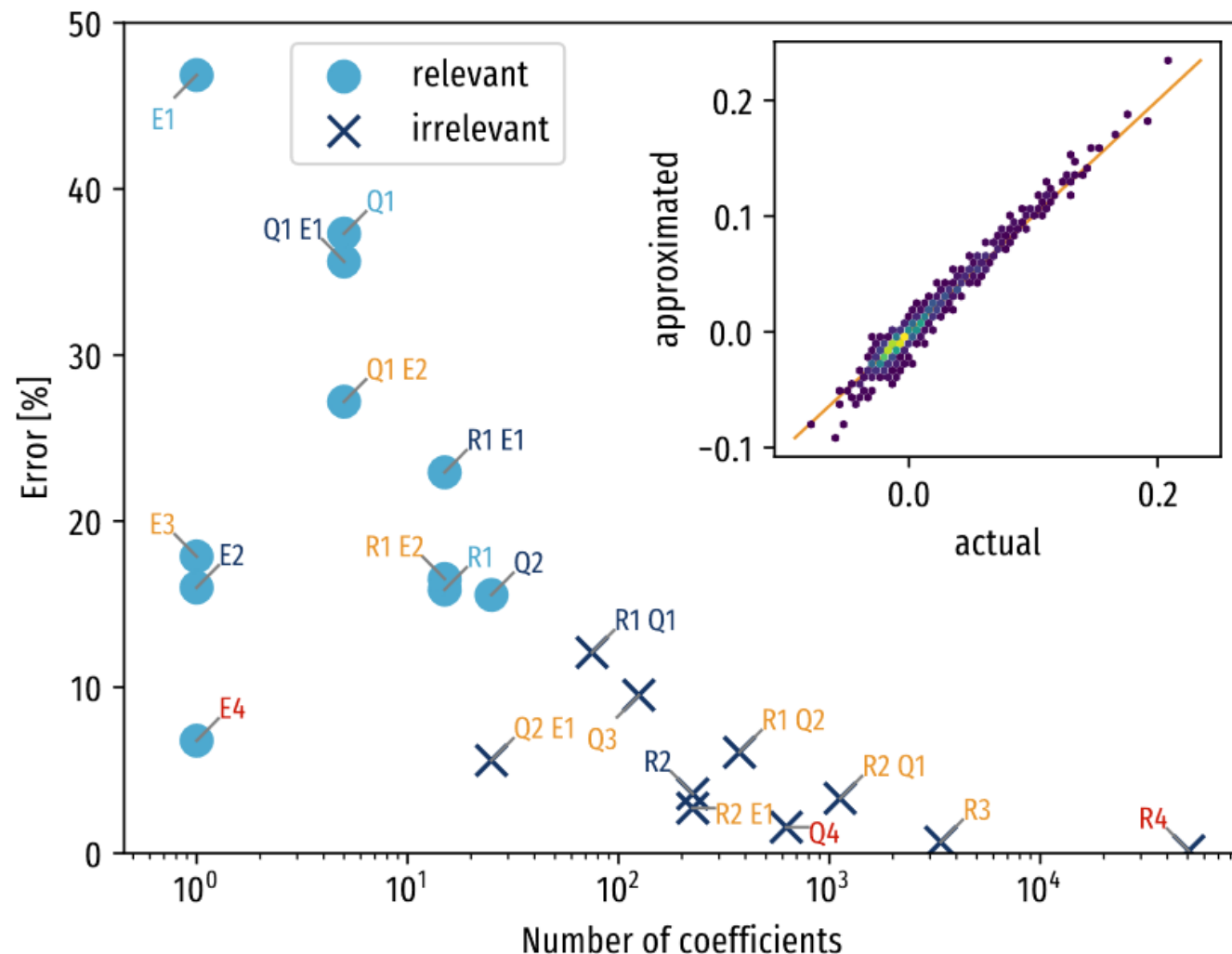
- Expensive terms also irrelevant
- For molecules, subset only
- Allows for efficient stencil design

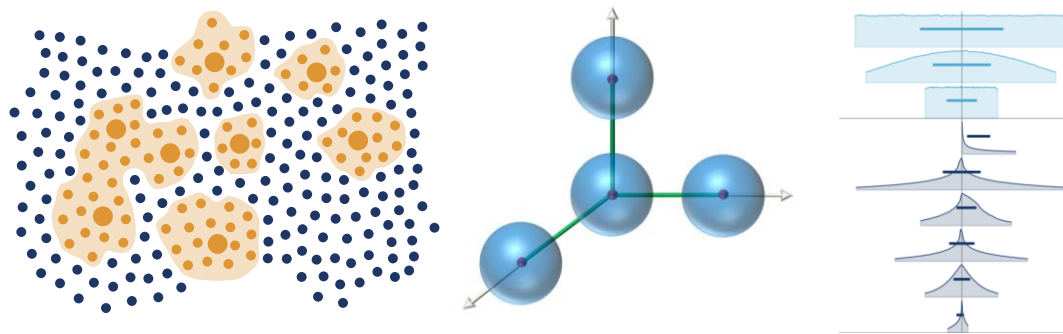
Estimated speedup „as is“

$$\frac{3^N}{N^2 + 12N - 1}$$

Lessons learned

- Many terms not relevant
- Smaller displacement
- Iterative procedure necessary
- Inclusion of limit expressions?
- Variable transformations?





Accessible | Can be treated perturbatively

Interpretable | Investigate interaction relevance

Efficient | Even for few atom systems

Design | Iterative refinement for molecules

Thanks

Anton Artemyev

Boris Lagutin

Philipp Demekhin