Basis Sets

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- Set = multiple basis functions
	- s-orbital: 1 basis function
	- p-orbital: 3 basis functions (px, py, pz)
- Finite
- Big families
	- atom-centered
		- Slater-type orbitals (STO): expensive integrals
		- Gaussian-type orbitals (GTO)
			- Primitive gaussian functions build up orbitals
	- plane waves
	- Wavelets
		- Systematically improving, rare
- Typically defined per element: problem for quantum alchemy
- Connection locality and cost
- Minimal basis set: one basis function for each orbital
- Polarization functions: asymmetry close to the nucleus: bonds
- Diffuse functions: asymmetry away from the nuclei: hydrogen bond, dipoles

Plane waves and the set of the set

- Path to complete basis set (CBS limit)
- Easy and elegant implementation except HF
- Easy derivatives
- Requires "fake" boundary conditions
- Empty space is not free
- Pseudopotentials required as cutoff too high
- Commonly used for materials

Atom-centered basis functions and the mass of 104

- Localised, so empty space is free
- Scales linearly with number of atoms
- Numerical issues if atoms close together
- Any boundary conditions possible
- No path to complete basis set limit: empirical schemes necessary
- Harder to implement
- Commonly used for molecules / mixed settings

Real-Space

- Multi-dimensional grid
- Easiest to approach CBS
- Hard to implement
- Slow in evaluation
- Mostly used for technical demonstrations / settling one-off questions

Wavelets

- Finite Support: easy to subdivide
- Niche implementations
- Unclear whether "best of both worlds" or "worst of both worlds"
- Gaussian-type orbitals
	- Sum of Gaussians form one orbital: contraction
- Minimal basis set: "single zeta" (Zeta commonly used for the exponent in STO-nG)
- Twice/three times the basis functions for valence atomic orbitals: double-zeta, triple-zeta, ...
- Split valence (single zeta for core, multiple for valence)

 $6 - 31 + 6^{**}$

- 6 One core basis function with 6 contracted Gaussians
- 31 Two valence basis functions with 3 and 1 contracted Gaussian respectively
- * Polarization on heavy atoms
- ** Polarization also on hydrogen atoms
- + Diffuse functions on heavy atoms
- ++ Diffuse function also on hydrogen atoms

aug-cc-cpCVDZ

aug Diffuse functions p Polarization functions DZ Double zeta C core basis functions

 $(6s,3p) \to [2s,1p]$

Contraction: (primitives) -> [basis functions]

Question: [3s2p1d] is how many basis functions? Question: Ar with electron configuration [1s² 2s² 2p⁶ 3s² 3p⁶] in cc-pVTZ has how many basis functions?

Molecule setup

```
mol_h2o = gto.M(atom = '0 0 0 0; H 0 1 0; H 0 0 1', basis = 'copvdz')
```

```
from pyscf import scf
rhf_h2o = scf.RHF(mol_h2o)e_h20 = rhf_h20.kernel()
```
Electron density in ao basis

```
dm1 ao = calc.make rdm1()
```
Electron density on a grid

```
grid = pyscf.dft.gen grid.Grids(mol)grid<math>.level = 3grid.build()
ao_value = pyscf.dft.numint.eval_ao(mol, grid. coords, deriv=0)rho = pyscf.dft.numint.eval rho(mol, ao value, dm1 ao, xctype="LDA")
```